## DIBELS Math

## DIBELS ${ }^{\circ}$ Math

## Essential Workshop

## Workshop Objectives

- Understand the research behind DIBELS Math
- Learn how to give and score DIBELS Math
- Begin to link DIBELS Math to Vmath Summer


## Workshop Agenda

## Part 1: DIBELS Math Foundations

Part 2: Beginning Quantity Discrimination (BQD)
Part 3: Number Identification Fluency (\#IDF)
Part 4: Next Number Fluency (N\#F)
Part 5: Advanced Quantity Discrimination (AQD)
Part 6: Missing Number Fluency (?\#F)
Part 7: Computation (C) Test, Score, Response Pattern Analysis
Part 8: Concepts \& Applications (C\&A) Test, Score, Response Pattern Analysis
Part 9: Common Core State Standards \& Vmath Modules
Part 10: Next Steps... Follow-up Workshop in PM for Early Numeracy Skills

## DIBELS ${ }^{\circ}$ Math is One Part of an Effective School-wide System

Curriculum and<br>Goal<br>Assessment Instruction<br>Student Success<br>$100 \%$ of Students will meet goals

Numeracy
Environment and Resources

## Key Features of DIBELS ${ }^{\circ}$ Math

- Universal Screening and Progress Monitoring
- Standardized
- Timed
- Brief
- Simple Scoring
- Predictive-Benchmark Goals \& Composite Scores


## DIBELS® Math Measures

## Early Numeracy

-Beginning Quantity Discrimination

- Number Identification Fluency
-Next Number Fluency
-Advanced Quantity Discrimination
-Missing Number Fluency
Computation
Concepts and Applications


## Measures by Grade

|  | Beginning Quantity Discrimination | Number Identification | Next <br> Number <br> Fluency | Advanced Quantity Discrimination | Missing Number Fluency | Computation | Concepts and Apolications |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| K |  |  |  |  |  |  |  |
| $1^{\text {st }}$ |  |  |  |  |  |  |  |
| $2^{\text {nd }}$ |  |  |  |  |  |  |  |
| $3^{\text {rd }}$ |  |  |  |  |  |  |  |
| $4^{\text {th }}$ |  |  |  |  |  |  |  |
| $5^{\text {th }}$ |  |  |  |  |  |  |  |
| $6^{\text {th }}$ |  |  |  |  |  |  |  |

## DIBELS® Math Benchmark Goals

## What is a Benchmark Goal?

A research-based target score:

- Represents the lowest level of performance on a measure that predicts reaching the next goal
- Consists of three parts: a basic early numeracy skill, a level of performance, and a point in time
- If a student achieves a benchmark goal, the odds are in favor of that student achieving later mathematics outcomes.


## How are the Benchmark Goals derived?

Based on longitudinal research examining how a score on a measure at a point in time predicts later math outcomes

## Three Levels of Performance Compared to Benchmark Goals

If a student achieves a Benchmark Goal, the odds are in favor of that student achieving later mathematics outcomes.

- At or Above Benchmark: Odds are generally $80 \%$ to $90 \%$ of achieving subsequent benchmark goals and important mathematics outcomes. Student is likely to make adequate progress with effective core instruction.
- Below Benchmark: Odds are generally $40 \%$ to $60 \%$ of achieving subsequent benchmark goals and important mathematics outcomes. Student is likely to need strategic support to make adequate progress.
- Well Below Benchmark: Odds are generally 10\% to 20\% of achieving subsequent benchmark goals and important mathematics outcomes. Student is likely to need intensive support to make adequate progress.


## Benchmark Goals and Local Norms

- Benchmark Goals are available for the

Early Numeracy measures and Computation ( $1^{\text {st }}, 2^{\text {nd }}, 4^{\text {th }}$, and $5^{\text {th }}$ grade)

- Schools should use local normative information, available through DIBELSnet, for Computation and Concepts \& Applications and in $3^{\text {rd }}$ and $6^{\text {th }}$ grade while the Benchmark Goals are developed during the 2014-2015 school year.


## Interpreting Results: Local Norms

Local norms look at a student's performance relative to your school/district

- $1 / 2$ of the students will be at or below average and $1 / 2$ of the students will be at or above average
- The average only applies to your school/district
- Demographics of your school/district must be taken into account when examining performance
- Other districts may be higher or lower

The magnitude of the discrepancy can be used to determine whether intervention is necessary, and to set instructional goals.
Use the following rule of thumb:

- $<20 \%$ ile $=$ at risk
- 20 \%ile-40\%ile = some risk
- > 40 \%ile = low risk


## Composite Scores

- Composite scores provide the best overall estimate of the student's skills.
- Composite scores take all of the measures into consideration.
- Different weights are given to different measures depending on the time of year.
- Composite scores may increase or decrease because the number of measures included may vary (e.g. $1^{\text {st }}$ grade from fall to winter).


## Linkages to Math Research

- Early Numeracy based on foundational skills required to develop number sense
- Number sense involves basic "intuitions" and ideas about numbers (Lee et al., 2008)
- includes the ability to compare the magnitude of numbers, to understand the relative effect of arithmetical operations on numbers, and to have meaningful referents for number and quantity (NCTM, 1989)
- Although hard to define, number sense predicts academic achievement (Berch, 2005; Gersten et al., 2005)
- Number sense has been operationalized in various ways (see Lago \& DiPerna, 2010)


## DIBELS Math

## Part 2- BQD Beginning Quantity Discrimination

## DIBELS ${ }^{\circ}$ Math

| Underlying Concepts | DIBELS Math Measures |
| :--- | :--- |
| Magnitude Comparison | Beginning Quantity Discrimination <br> Advanced Quantity Discrimination |
| Subitization | Beginning Quantity Discrimination <br> (indirectly measured) |
| Strategic Counting | Next Number Fluency <br> Missing Number Fluency |
| Number Identification | Number Identification |
| Basic Computation | Computation |

## Magnitude Comparison

What is it?
-Students' ability to discern quickly the greatest number in a set and ability to weigh relative differences in magnitude efficiently (Gersten et al., 2012)
-Requires understanding of place value and ability to perform mental calculations
-Complexity of items depends on the set of numbers given to the student
Why is it important?

- It is related to other critical areas of mathematical performance such as mental calculation and place value (Gersten et al., 2012).


## What Is Subitization?

- The ability to instantly judge the number associated with a group of items.
- Different from counting
- Children as young as 2 begin to subitize small amounts
- Conceptual subitizing plays an advanced organizing role (Clements, 1999)
- For example, with the domino pattern students who are able to conceptually subitize recognize the number pattern as composite parts and as a whole


## Why Is Subitization Important?

- Thought to be an important precursor to mathematics development
- Recent studies have linked subitizing ability to counting, arithmetic, and number system knowledge.
- Research has found that there is a significant link between subitizing ability and mathematical skills in kindergarten aged children (Yun et. al., 2011).
- Predictive of later mathematics
performance (Desoete \& Gregorie, 2006)


## Beginning Quantity Discrimination

Skill Magnitude Comparison and Subitization (indirectly)

## Administration <br> Time

Administration
Schedule
BOY K to EOY K

Score 1 point for each correctly identified number

Wait Rule
If the student does not respond within 3 seconds on an item, provide the correct answer and mark a slash (/) through the number.

Discontinue Rule 0 points in the first four items (the first page)

## Preliminary BQD Benchmark Goals

| Grade | Score <br> Level | Need for <br> Support | BOY | MOY | EOY |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | At or Above | Core | 5 | 8 | 11 |
|  | Below | Strategic | $2-4$ | $4-7$ | $7-10$ |
|  | Well Below | Intensive | $0-1$ | $0-3$ | $0-6$ |

## Beginning Quantity Discrimination Video

## DIBELS Math

## Part 3- \#IDF <br> Number Identification Fluency

## DIBELS ${ }^{\circ}$ Math

| Underlying Concepts | DIBELS Math Measures |
| :--- | :--- |
| Magnitude Comparison | Beginning Quantity Discrimination <br> Advanced Quantity Discrimination |
| Subitization | Beginning Quantity Discrimination <br> (indirectly measured) |
| Strategic Counting | Next Number Fluency <br> Missing Number Fluency |
| Number Identification | Number Identification Fluency |
| Basic Computation | Computation |

## Number Identification Fluency

What is it?
-Linking written numbers to names
-Equivalent to letter naming fluency in reading
Why is it important?
-Not necessarily a mathematical skill on its own, it serves as an important predictor of later skills.
-Number recognition is essential for later mathematical skills.

## Number Identification Fluency (\#IDF)

Skill Number Identification

## Administration <br> Time <br> 1 minute

## Administration Schedule

Beginning of kindergarten to beginning of first grade

Score 1 point for each correctly identified number

Wait Rule
If the student does not respond within 3 seconds on an item, provide the correct answer and mark a slash (/) through the number.

Discontinue Rule 0 points in the first five items (the first line)

## Preliminary \#IDF Benchmark Goals

| Grade | Score Level | Need for Support | BOY | MOY | EOY |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Kindergarten | At or Above | Core | 6 | 13 | 23 |
|  | Below | Strategic | 3-5 | 7-12 | 13-22 |
|  | Well Below | Intensive | 0-2 | 0-6 | 0-12 |
| First Grade | At or Above | Core | 27 |  |  |
|  | Below | Strategic | 15-26 |  |  |
|  | Well Below | Intensive | 0-14 |  |  |

## Number Identification Fluency Video

## DIBELS Math

## Part 4- NNF <br> Next Number Fluency

## DIBELS ${ }^{\circ}$ Math

| Underlying Concepts | DIBELS Math Measures |
| :--- | :--- |
| Magnitude Comparison | Beginning Quantity Discrimination <br> Advanced Quantity Discrimination |
| Subitization | Beginning Quantity Discrimination <br> (indirectly measured) |
| Strategic Counting | Next Number Fluency <br> Missing Number Fluency |
| Number Identification | Number Identification Fluency |
| Basic Computation | Computation |

## Strategic Counting

What is it?
-Knowledge of counting principles and skill in counting (Gersten et al., 2012)
-Examples include counting with reference to objects, counting on, being able to say counting words without reference to objects

Why is it important?
-It is a fundamental skill that leads to mathematical proficiency and understanding (Siegler \& Robinson, 1982)

Strategic counting is a critical problem solving skill (Gersten et al., 2012)

## Next Number Fluency

Skill Counting (extending the counting sequence)

Administration
Time
1 minute

Administration
Schedule
Beginning of kindergarten to beginning of first grade

Score 1 point for each correct number

Wait Rule
If the student does not respond within 3 seconds on an item, mark a slash (/) through the number.

Discontinue Rule 0 points in the first five items (the first line)

## Preliminary NNF Benchmark Goals

| Grade | Score <br> Level | Need for <br> Support | BOY | MOY | EOY |
| :---: | :---: | :--- | :---: | :---: | :---: |
|  | At or Above | Core | 5 | 10 | 12 |
|  | Below | Strategic | $2-4$ | $6-9$ | $9-11$ |
|  | Well Below | Intensive | $0-1$ | $0-5$ | $0-8$ |
|  | At or Above | Core | 12 |  |  |
| First Grade | Below | Strategic | $8-11$ |  |  |
|  | Well Below | Intensive | $0-7$ |  |  |

Next Number Fluency Video

## DIBELS Math

# Part 5- AQD <br> Advanced Quantity Discrimination 

## DIBELS ${ }^{\circ}$ Math

| Underlying Concepts | DIBELS Math Measures |
| :--- | :--- |
| Magnitude Comparison | Beginning Quantity Discrimination <br> Advanced Quantity Discrimination |
| Subitization | Beginning Quantity Discrimination <br> (indirectly measured) |
| Strategic Counting | Next Number Fluency <br> Missing Number Fluency |
| Number Identification | Number Identification |
| Basic Computation | Computation |

## Magnitude Comparison

What is it?
-Students' ability to discern quickly the greatest number in a set and ability to weigh relative differences in magnitude efficiently (Gersten et al., 2012)
-Requires understanding of place value and ability to perform mental calculations
-Complexity of items depends on the set of numbers given to the student

Why is it important?

- It is related to other critical areas of mathematical performance such as mental calculation and place value (Gersten et al., 2012).


## Advanced Quantity Discrimination

## Skill Magnitude Comparison

Administration
Time

## Administration <br> Schedule

Beginning of first grade to end of first grade

## Score

1 point for each correct number

If the student does not respond within 3 seconds on an
Wait Rule item, provide the correct answer and mark a slash (/) through the number

Discontinue Rule 0 points in the first six items (the first page)

## Preliminary AQD Benchmark Goals

| Grade | Score <br> Level | Need for <br> Support | BOY | MOY | EOY |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | At or Above | Core | 10 | 18 | 20 |
|  | Below | Strategic | $5-9$ | $13-17$ | $15-19$ |
|  | Well Below | Intensive | $0-4$ | $0-12$ | $0-14$ |

## Advanced Quantity Discrimination Video

## DIBELS Math

## Part 6- ?NF Missing Number Fluency

## DIBELS ${ }^{\circ}$ Math

| Underlying Concepts | DIBELS Math Measures |
| :--- | :--- |
| Magnitude Comparison | Beginning Quantity Discrimination <br> Advanced Quantity Discrimination |
| Subitization | Beginning Quantity Discrimination <br> (indirectly measured) |
| Strategic Counting | Next Number Fluency <br> Missing Number Fluency |
| Number Identification | Number Identification |
| Basic Computation | Computation |

## Strategic Counting

What is it?
-Knowledge of counting principles and skill in counting (Gersten et al., 2012)
-Examples include counting with reference to objects, counting on, being able to say counting words without reference to objects

Why is it important?
-It is a fundamental skill that leads to mathematical proficiency and understanding (Siegler \& Robinson, 1982).
-Strategic counting is a critical problem solving skill (Gersten et al., 2012).
-Allows for flexibility in mental computing

## Missing Number Fluency (MNF)

| Skill | Strategic Counting (extending the counting sequencecounting by $1 \mathrm{~s}, 5 \mathrm{~s}, 10 \mathrm{~s}$ ) |
| :---: | :---: |
| Administration Time | 1 minute |
| Administration Schedule | Beginning of first grade to end of first grade |
| Score | 1 point for each correct number |
| Wait Rule | If the student does not respond within 5 seconds on an item, provide the correct answer and mark a slash (/) through the number. |
| Discontinue Rule | 0 points in the first six items |

## Preliminary MNF Benchmark Goals

| Grade | Score <br> Level | Need for <br> Support | BOY | MOY | EOY |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | At or Above | Core | 4 | 7 | 9 |
|  | Below | Strategic | $2-3$ | $5-6$ | $7-8$ |
|  | Well Below | Intensive | $0-1$ | $0-4$ | $0-6$ |

## Missing Number Fluency

## DIBELS Math

Part 7
Computation

## DIBELS ${ }^{\circ}$ Math

| Underlying Concepts | DIBELS Math Measures |
| :--- | :--- |
| Magnitude Comparison | Beginning Quantity Discrimination <br> Advanced Quantity Discrimination |
| Subitization | Beginning Quantity Discrimination <br> (indirectly measured) |
| Strategic Counting | Next Number Fluency <br> Missing Number Fluency |
| Number Identification | Number Identification |
| Basic Computation | Computation |

## Basic Computation

## What is it?

-Addition
-Subtraction
-Multiplication
-Division
Why is it important?
-NAEP results in 2011 indicate that $40 \%$ of fourth grade students are at or above proficient (National Center for Education Statistics, 2011).
-40\% of the NAEP assessment in 4th grade focuses on number properties and operations, which are computation problems.
-Math computation plays a role in overall math achievement.

## Computation

## Skill Basic Computation

## Administration <br> Time <br> $2,3,5,6$ minutes per worksheet depending on grade

Administration Schedule

Beginning of first grade to end of sixth grade

Score Correct digits in final answer

Wait Rule No wait rule

Discontinue Rule No discontinue rule

## Preliminary Computation Benchmark Goals

| Grade | Score <br> Level | Need for <br> Support | BOY | MOY | EOY |
| :---: | :--- | :--- | :---: | :---: | :---: |
|  | At or Above | Core | 5 | 9 | 13 |
|  | Below | Strategic | $2-4$ | $5-8$ | $9-12$ |
|  | Well Below | Intensive | $0-1$ | $0-4$ | $0-8$ |
| Second <br> Grade | At or Above | Core | 7 | 10 | 13 |
|  | Below | Strategic | $4-6$ | $7-9$ | $10-12$ |
|  | Well Below | Intensive | $0-3$ | $0-6$ | $0-9$ |
| Third Grade | Use L_ocal |  |  |  |  |

## Preliminary Computation Benchmark Goals

| Grade | Score <br> Level | Need for <br> Support | BOY | MOY | EOY |
| :--- | :--- | :--- | :--- | :---: | :---: |
| Fourth <br> Grade | At or Above | Core | 18 | 29 | 42 |
|  | Below | Strategic | $13-17$ | $21-28$ | $31-41$ |
|  | Well Below | Intensive | $0-12$ | $0-20$ | $0-30$ |
|  | At or Above | Core | 29 | 48 | 53 |
| Fifth Grade | Below | Strategic | $16-28$ | $31-47$ | $37-52$ |
|  | Well Below | Intensive | $0-15$ | $0-30$ | $0-36$ |
|  |  |  |  |  |  |
| Sixth Grade | Use Local Norms |  |  |  |  |

## Grade Level Time Limits for Computation Worksheets

| Grade | Time Limit Per <br> Worksheet | Total Time for <br> Benchmark Assessment <br> (2 Worksheets) |
| :---: | :---: | :---: |
| 1 and 2 | 2 minutes | 4 minutes |
| 3 | 3 minutes | 6 minutes |
| 4 | 5 minutes | 10 minutes |
| 5 | 6 minutes | 12 minutes |
| 6 | 6 minutes | 12 minutes |

## Practice Activity: Take the Test!

DIBELS ${ }^{\circledR}$ Math Early Release / Computation Grade 4
Benchmark 3 / Form B

| 1. $\begin{array}{r} 882 \\ +\quad 16 \\ \hline 898 \end{array}$ | 2. $\begin{array}{r} 118 \text { '54 } \\ +1778 \\ \hline 3632 \end{array}$ | 3. $5 \frac{1}{3}+1 \frac{1}{3}=6 \frac{2}{6}$ | 4. $\begin{array}{r} 9 \\ \times 7 \\ \hline 63 \end{array}$ | 5. $\begin{gathered} 42 \\ 4 \longdiv { 7 3 8 } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: |
| 6. $\begin{array}{r} 672 \\ -332 \\ \hline 340 \end{array}$ | 7. $\frac{5}{6}-\frac{2}{6}=\frac{3}{6}$ | 8. $\begin{array}{r} 7126 \\ -\quad 638 \\ \hline 7512 \end{array}$ | 9. $\begin{array}{r} 79 \\ \times 11 \\ \hline 79 \\ \times 79 \\ \hline 869 \end{array}$ | 10. $6 \frac{5}{8}+5 \frac{2}{8}=\\| \frac{7}{8}$ |
| $\begin{array}{ll} \hline 11 . & 80 \\ & 2 \longdiv { 6 2 7 } \end{array}$ | 12. $\stackrel{3}{7}{ }_{21}$ | $\text { 13. } \begin{array}{r} 3 \\ 98 \\ \times 48 \\ \sqrt{768} \\ \hline 4920 \\ \hline 4688 \end{array}$ | $\frac{14}{14}+\frac{1}{4}=$ | 15. $\begin{array}{r} 253 \\ \times \quad 6 \\ \hline \end{array}$ |

## Practice Activity: Score

DIBELS ${ }^{\ominus}$ Math Early Release / Computation Grade 4 Benchmark 3 / Form B

Total:

| 1. $\begin{array}{r} 882 \\ +\quad 16 \\ \hline 898 \end{array}$ <br> $\uparrow \uparrow \uparrow$ <br> (3) | 2. $\begin{array}{r} 118 ' 54 \\ +1778 \\ \hline 3632 \\ \uparrow \uparrow \uparrow \uparrow \end{array}$ | 3. $5 \frac{1}{3}+1 \frac{1}{3}=6 \frac{1}{6}$ <br> (2) | 4. $\begin{array}{r} 9 \\ \times 7 \\ \hline 63 \end{array}$ <br> (2) | 5. $\begin{gathered} 42 \\ 4 \longdiv { 7 3 8 } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: |
| 6. $\begin{array}{r} 672 \\ -332 \\ \hline 340 \end{array}$ <br> (3) | 7. $\frac{5}{6}-\frac{2}{6}=\frac{3}{6}$ | 8. $\begin{array}{r} 7126 \\ -\quad 638 \\ \hline 7512 \end{array}$ | 9. $\begin{array}{r} 79  \tag{8}\\ \times 11 \\ 179 \\ \times 790 \\ \hline 869 \end{array}$ | 10. $6 \frac{5}{8}+5 \frac{2}{8}=\\| \frac{7}{8}$ <br> (4) |
| $\begin{array}{rr}\text { 11. } & 80 \\ & 2 \longdiv { 6 2 7 }\end{array}$ | 12. $\frac{3}{7 \longdiv { 2 1 }}$ | 13. $\begin{array}{r} 38 \\ 98 \\ \times 48 \\ \frac{3988}{768} \\ \hline 4688 \end{array}$ | 14. $\frac{1}{4}+\frac{1}{4}=$ | 15. $\begin{array}{r} 253 \\ \times \quad 6 \\ \hline \end{array}$ |

## Response Pattern Analysis

- Student Computation Worksheet(s)
- Benchmark Scoring Booklet
* Note the last item attempted
* Circle Correct Items
* Put X on Incorrect Items
* Leave Blank Skipped or Not Attempted Items


## DIBELS Math

## Part 8-C\&A Concepts and Applications

## Concepts and Applications

What is it?
-A standardized measure designed to assess students' progress in the basic skills of understanding mathematical concepts and vocabulary and applying that knowledge to solve mathematical problems. It can be administered individually or to groups.

## Concepts and Applications

| Skill | Understanding math concepts and vocabulary, and <br> applying that knowledge to solving problems |
| ---: | :--- |
| Administration | $5,10,12,14$ or 16 minutes per worksheet depending on <br> grade |
| Administration <br> Schedule | Beginning of second grade to end of sixth grade |
| Score | Correct digits in final answer, exact answer points per <br> box, exact answer points per line, or exact answer points <br> per segment |
| Wait Rule | No wait rule |
| Discontinue Rule | No discontinue rule |

## Grade Level Time Limits for Worksheets

| Grade | Time Limit |
| :---: | :---: |
| 2 | 5 minutes |
| 3 | 12 minutes |
| 4 | 10 minutes |
| 5 | 14 minutes |
| 6 | 16 minutes |

## Concepts and Applications

- Practice Activity: Take the Test!
- Practice Activity: Score
- Response Pattern Analysis
-Student Concepts \& Applications Worksheet
-Benchmark Scoring Booklet
* Note the last item attempted
* Circle Correct Items
* Put X on Incorrect Items
* Leave Blank Skipped or Not Attempted Items


## DIBELS Math

## Part 9

Common Core State Standards \& Vmath Summer Modules

## DIBELS Math

Part 10
Conclusion \& Next Steps

